

Application of detailed quantum  
codes  
in the evaluation of rare gas ions  
radiative transition probabilities

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## INTRODUCTION

Radiative transition probabilities of rare gas ions  
to do spectral analysis of fusion plasmas, especially Ar  
and Xe

Collection of data available for various ionisation  
stages of Ar

ArI, ArII, ArIII, ArIV

Recent work: Radiative transition probabilities:

ArII: Multiplet 5s-5p

ArIII: Multiplet 4d-4p

ArIV: Multiplet 4p-4s

## **DATA and CODES**

### DATA:

#### FOR ATOMIC STRUCTURE

Energy levels

Oscillator strengths

Wavelengths

Transition probabilities for ArII, ArIII, ARIV

### CODES:

#### FOR ATOMIC STRUCTURE

Hartree Fock OPM (1)

Dirac Fock SICODIFO (2)

SUPERSTRUCTURE SST (3)

FAC(4)

## RESULTS

### Ab.Initio Calculation: SUPERSTRUCTURE

Energy levels, line strengths, weighted oscillator strengths and radiative transition probabilities are calculated in LSJ coupling using the SUPERSTRUCTURE code (SST), (3) which is well suited for the computation of large quantities of atomic data for multiplied ions.

In the first step, wave function are determined by diagonalization of the non-relativistic Hamiltonian using orbitals calculated in Thomas-Fermi-Dirac-Amaldi potentials. The scaling parameters are obtained by a self-consistent minimization procedure.

In the second step RELATIVISTIC corrections (spin-orbit, mass, Darwin and one body) are introduced according to the Breit-Pauli approach. The results are obtained in LS and LSJ couplings.

Results for ArII 5s-5p, ArIII 4d-4p, ArIV 4p-4s multiplets in LSJ coupling are presented

[14]  $A_{j \rightarrow i} / \text{Ar II} / 5s \leftarrow 5p$  Transition Probabilities in  $10^7 \text{s}^{-1}$

CbA											SST			LANL									
5s-5p	Term	$E_j$ (cm $^{-1}$ )	Term	$\lambda$ [Å]	$L_i$	$J_i$	$S_i$	$L_{ei}$	$L_j$	$J_j$	$S_j$	$2J_j+1$	$A_{j \rightarrow i}$	$E_i$ (cm $^{-1}$ )	$E_j$ (cm $^{-1}$ )	$\lambda$ [Å]	$A_{j \rightarrow i}$	$E_i$ (cm $^{-1}$ )	$E_j$ (cm $^{-1}$ )	$\lambda$ [Å]	$A_{j \rightarrow i}$		
<b>5s, 5p <math>^3P_2 (+ e^- \rightarrow \text{doublet, quartet})</math></b>																							
1	$^4P_{5/2}$	181594.14	$^4P_{5/2}$	13942.98	1	2.5	1.5	1	1	2.5	1.5	6	1.13	182459	189384	14438	1.37						
2			$^4P_{3/2}$	13428.60	1	2.5	1.5	1	1	1.5	1.5	4	0.81		189655	13895	1.20						
3			$^4D_{7/2}$	12786.27	1	2.5	1.5	1	2	3.5	1.5	8	2.06		190129	13037	2.06						
4			$^2P_{1/2}$	11989.70	1	2.5	1.5	1	1	0.5	0.5	2			193227								
5			$^2D_{5/2}$	11214.37	1	2.5	1.5	1	2	2.5	0.5	6			198267								
6			$^2P_{3/2}$	11113.47	1	2.5	1.5	1	1	1.5	0.5	4			192933								
7	$^2P_{3/2}$	183090.89	$^4P_{5/2}$	17620.15	1	1.5	0.5	1	1	2.5	1.5	6		184255	189384								
8			$^4P_{3/2}$	16806.61	1	1.5	0.5	1	1	1.5	1.5	4			189655								
9			$^4D_{7/2}$	15812.43	1	1.5	0.5	1	2	3.5	1.5	8			190129								
10			$^2P_{1/2}$	14611.89	1	1.5	0.5	1	1	0.5	0.5	2	0.50		193227	11145	0.21						
11			$^2D_{5/2}$	13476.40	1	1.5	0.5	1	2	2.5	0.5	6	1.88		198267								
12			$^2P_{3/2}$	13330.95	1	1.5	0.5	1	1	1.5	0.5	4	1.62		192933	11522	1.67						
<b>5s, 5p <math>^3P_1 (+ e^- \rightarrow \text{doublet, quartet})</math></b>																							
13	$^4P_{3/2}$	182222.12	$^4P_{1/2}$	13858.82	1	1.5	1.5	1	1	0.5	1.5	2	1.34	183135	190020	14525	1.36						
14			$^4D_{5/2}$	13454.01	1	1.5	1.5	1	2	2.5	1.5	6	1.23		190491	13593	1.47						
15			$^2S_{1/2}$	11467.10	1	1.5	1.5	1	0	0.5	0.5	2			191759	11595	0.05						
16			$^2D_{3/2}$	11376.18	1	1.5	1.5	1	2	1.5	0.5	4			191766								
17			$^4S_{3/2}$	11176.33	1	1.5	1.5	1	0	1.5	1.5	4	0.96		191975	11311	1.06						
18	$^2P_{1/2}$	183914.64	$^4P_{1/2}$	18105.77	1	0.5	0.5	1	1	0.5	1.5	2		185102	190020								
19			$^4D_{5/2}$	17420.96	1	0.5	0.5	1	2	2.5	1.5	6			190491								
20			$^2S_{1/2}$	14228.64	1	0.5	0.5	1	0	0.5	0.5	2	0.53		191759	15022	0.09						
21			$^2D_{3/2}$	14088.91	1	0.5	0.5	1	2	1.5	0.5	4	1.37		191766	15007	0.73						
22			$^4S_{3/2}$	13783.67	1	0.5	0.5	1	0	1.5	1.5	4			191975	14549	0.02						
<b>5s, 5p <math>^3P_0 (+ e^- \rightarrow \text{quartet})</math></b>																							
23	$^4P_{1/2}$	182951.26	$^4D_{3/2}$	13976.16	1	0.5	1.5	1	2	1.5	1.5	4	0.66	183684	190994	13678	0.83						
24			$^4D_{1/2}$	12850.56	1	0.5	1.5	1	2	0.5	1.5	2	1.68		191267	13187	1.85						

[14]  $A_{i \rightarrow j} / \text{Ar II} / 5s \leftarrow 5p$  Transition Probabilities in  $10^7 \text{s}^{-1}$

										SST				LANL								
CbA										SST				LANL								
$5s-5p$	Term	$E_i$ (cm $^{-1}$ )	Term	$\lambda$ [Å]	$L_i$	$J_i$	$S_i$	$l_{e_j}$	$L_j$	$J_j$	$S_j$	$2J_j+1$	$A_{i \rightarrow j}$	$E_i$ (cm $^{-1}$ )	$E_j$ (cm $^{-1}$ )	$\lambda$ [Å]	$A_{i \rightarrow j}$	$E_i$ (cm $^{-1}$ )	$E_j$ (cm $^{-1}$ )	$\lambda$ [Å]	$A_{i \rightarrow j}$	
<b><math>5s, 5p \ ^1D_2 (+ e^- \rightarrow \text{doublet})</math></b>																						
25	$^4D_{5/2}$	195864.73	$^2P_{3/2}$	13999.56	2	2.5	0.5	2	1	1.5	0.5	4	1.45	198267	206481	12174	2.43					
26			$^2F_{5/2}$	13723.95	2	2.5	0.5	2	3	2.5	0.5	6	0.11		205263	14293	0.13					
27			$^4F_{7/2}$	13637.28	2	2.5	0.5	2	3	3.5	0.5	8	1.74		205310	14187	1.59					
28			$^2P_{1/2}$	12937.25	2	2.5	0.5	2	1	0.5	0.5	2			206668							
29			$^4D_{3/2}$	12122.64	2	2.5	0.5	2	2	1.5	0.5	4	0.24		206308	12435	0.03					
30			$^2D_{5/2}$	12092.86	2	2.5	0.5	2	2	2.5	0.5	6	2.25		206364	12349	2.22					
31	$^4D_{3/2}$	195866.84	$^2P_{3/2}$	14003.70	2	1.5	0.5	2	1	1.5	0.5	4	0.16	198269	206481	12178	0.04					
32			$^2F_{5/2}$	13727.93	2	1.5	0.5	2	3	2.5	0.5	6	1.59		205263	14298	1.43					
33			$^4F_{7/2}$	13641.21	2	1.5	0.5	2	3	3.5	0.5	8			205310							
34			$^2P_{1/2}$	12940.78	2	1.5	0.5	2	1	0.5	0.5	2	2.01		206668	11908	0.26					
35			$^4D_{3/2}$	12125.74	2	1.5	0.5	2	2	1.5	0.5	4	2.15		206308	12438	2.33					
36			$^2D_{5/2}$	12095.95	2	1.5	0.5	2	2	2.5	0.5	6	0.16		206364	12353	0.20					
<b><math>5s, 5p \ ^1S_0 (+ e^- \rightarrow \text{doublet})</math></b>																						
37	$^2S_{1/2}$	220456.00	$^2P_{3/2}$	13175.23	0	0.5	0.5	0	1	1.5	0.5	4	2.28	220456	228046	13175	1.99					
38			$^2P_{1/2}$	13194.35	0	0.5	0.5	0	1	0.5	0.5	2	2.27		228035	13194	1.98					

En épais  $\rightarrow$  énergie provenant des calculs de SST.

[3] /  $A_{j \rightarrow i}$  / Ar IV /  $4s \leftarrow 4p$  Transition Probabilities in  $10^7 s^{-1}$

CbA										SST				LANL						
4s-4p	$E_i$ (cm $^{-1}$ )	Term	$E_j$ (cm $^{-1}$ )	Term	$\lambda$ [Å]	$L_i$	$J_i$	$S_i$	$I_{ci}$	$L_j$	$J_j$	$S_j$	$A_{j \rightarrow i}$	$E_i$ (cm $^{-1}$ )	$\lambda$ [Å]	$A_{j \rightarrow i}$	$E_j$ (cm $^{-1}$ )	$\lambda$ [Å]	$A_{j \rightarrow i}$	
<b><math>4s, 4p \ ^3P_2 (+e^- \rightarrow \text{doublet, quartet})</math></b>																				
1	251966.5	$^4P_{5/2}$	289829.8	$^4P_{5/2}$	2641.08	1	2.5	1.5	1	1	2.5	1.5	21.97	261981	299517	2664	27.85			
2			289233.2	$^4P_{3/2}$	2683.36	1	2.5	1.5	1	1	1.5	1.5	13.46		299005	2700	15.07			
3			287550.3	$^4D_{7/2}$	2810.27	1	2.5	1.5	1	2	3.5	1.5	25.98		296895	2864	29.67			
4			291662.1	$^2D_{5/2}$	2519.17	1	2.5	1.5	1	2	2.5	0.5			302983	2438	0.94			
5			295667.8	$^2P_{1/2}$	2288.26	1	2.5	1.5	1	1	0.5	0.5			328498					
6			295800.4	$^2P_{3/2}$	2281.34	1	2.5	1.5	1	1	1.5	0.5			329210					
7	257342.3	$^2P_{3/2}$	289829.8	$^4P_{5/2}$	3078.11	1	1.5	0.5	1	1	2.5	1.5		270381	299517	3432	0.27			
8			289233.2	$^4P_{3/2}$	3135.69	1	1.5	0.5	1	1	1.5	1.5			299005	3493	0.02			
9			287550.3	$^4D_{7/2}$	3310.38	1	1.5	0.5	1	2	3.5	1.5			296895					
10			291662.1	$^2D_{5/2}$	2913.77	1	1.5	0.5	1	2	2.5	0.5	24.41		302983	3067	16.89			
11			295667.8	$^2P_{1/2}$	2609.23	1	1.5	0.5	1	1	0.5	0.5	11.36		328498	1720	15.16			
12			295800.4	$^2P_{3/2}$	2600.23	1	1.5	0.5	1	1	1.5	0.5	28.71		329210	1699	30.68			
<b><math>4s, 4p \ ^3P_1 (+e^- \rightarrow \text{doublet, quartet})</math></b>																				
13	250901.4	$^4P_{3/2}$	289121.4	$^4P_{1/2}$	2616.43	1	1.5	1.5	1	1	0.5	1.5	26.95	261098	298754	2655	31.75			
14			286747.4	$^4D_{5/2}$	2789.71	1	1.5	1.5	1	2	2.5	1.5	18.63		296104	2856	23.15			
15			290250.4	$^2D_{3/2}$	2541.36	1	1.5	1.5	1	2	1.5	0.5			325128	1561	0.02			
16			291742.8	$^4S_{3/2}$	2448.50	1	1.5	1.5	1	0	1.5	1.5	13.16		310391	2028	28.69			
17			<b>282616.0</b>	$^2S_{1/2}$	3153.12	1	1.5	1.5	1	0	0.5	0.5			291626	3216	0.18			
18	256086.4	$^2P_{1/2}$	289121.4	$^4P_{1/2}$	3027.09	1	0.5	0.5	1	1	0.5	1.5		269329	298754	3398	0.08			
19			286747.4	$^4D_{5/2}$	3261.47	1	0.5	0.5	1	2	2.5	1.5			296104					
20			290250.4	$^2D_{3/2}$	2927.06	1	0.5	0.5	1	2	1.5	0.5	20.06		325128	1792	30.12			
21			291742.8	$^4S_{3/2}$	2804.55	1	0.5	0.5	1	0	1.5	1.5			310391					
22			<b>282616.0</b>	$^2S_{1/2}$	3769.38	1	0.5	0.5	1	0	0.5	0.5	3.69		291626	4484	2.89			
<b><math>4s, 4p \ ^3P_0 (+e^- \rightarrow \text{quartet})</math></b>																				
23	250214.6	$^4P_{1/2}$	286224.2	$^4D_{3/2}$	2777.04	1	0.5	1.5	1	2	1.5	1.5	11.25	260540	295530	2857	14.40			
24			285956.2	$^4D_{1/2}$	2797.86	1	0.5	1.5	1	2	0.5	1.5	22		295185	2886	24.97			

[3] /  $A_{j \rightarrow i}$  / Ar IV /  $4s \leftarrow 4p$  Transition Probabilities in  $10^7 s^{-1}$

										SST				LANL				
CbA										$E_i$ (cm $^{-1}$ )	$E_j$ (cm $^{-1}$ )	$\lambda[\text{\AA}]$	$A_{j \rightarrow i}$	$E_i$ (cm $^{-1}$ )	$E_j$ (cm $^{-1}$ )	$\lambda[\text{\AA}]$	$A_{j \rightarrow i}$	
4s-4p	$E_i$ (cm $^{-1}$ )	Term	$E_j$ (cm $^{-1}$ )	Term	$\lambda[\text{\AA}]$	$L_i$	$J_i$	$S_i$	$l_{ci}$	$L_j$	$J_j$	$S_j$	$A_{j \rightarrow i}$	$E_i$ (cm $^{-1}$ )	$E_j$ (cm $^{-1}$ )	$\lambda[\text{\AA}]$	$A_{j \rightarrow i}$	
<b>4s, 4p <math>^1D_2</math> (<math>+e^- \rightarrow</math> doublet)</b>																		
25	267760.9	$^2D_{3/2}$	303664.5	$^2F_{5/2}$	2785.24	2	1.5	0.5	2	3	2.5	0.5	25.26	280500	315486	2858	28.15	
26			303989.2	$^2F_{7/2}$	2760.27	2	1.5	0.5	2	3	3.5	0.5			315801			
27			311272.0	$^2P_{3/2}$	2298.26	2	1.5	0.5	2	1	1.5	0.5	4.81		329210	2052	12.77	
28			310982.0	$^2P_{1/2}$	2313.69	2	1.5	0.5	2	1	0.5	0.5	47.21		328498	2083	58.60	
29			305898.6	$^2D_{3/2}$	2622.08	2	1.5	0.5	2	2	1.5	0.5	29.25		325126	2240	40.36	
30			305826.6	$^2D_{5/2}$	2627.04	2	1.5	0.5	2	2	2.5	0.5	2.15		325067	2243	1.61	
31	267740.7	$^2D_{5/2}$	303664.5	$^2F_{5/2}$	2783.67	2	2.5	0.5	2	3	2.5	0.5	1.81	280478	315486	2856	2.30	
32			303989.2	$^2F_{7/2}$	2758.74	2	2.5	0.5	2	3	3.5	0.5	27.86		315801	2831	30.72	
33			311272.0	$^2P_{3/2}$	2297.20	2	2.5	0.5	2	1	1.5	0.5	43.39		329210	2052	50.98	
34			310982.0	$^2P_{1/2}$	2312.60	2	2.5	0.5	2	1	0.5	0.5			328498			
35			305898.6	$^2D_{3/2}$	2620.69	2	2.5	0.5	2	2	1.5	0.5	3.25		325126	2239	8.92	
36			305826.6	$^2D_{5/2}$	2625.64	2	2.5	0.5	2	2	2.5	0.5	30.2		325067	2242	45.07	
<b>4s, 4p <math>^1S_0</math> (<math>+e^- \rightarrow</math> doublet)</b>																		
37	288903.0	$^2S_{1/2}$	327311.0	$^2P_{3/2}$	2603.62	0	0.5	0.5	0	1	1.5	0.5	33.06	304670	343810	2394	41.16	
38			327147.0	$^2P_{1/2}$	2614.79	0	0.5	0.5	0	1	0.5	0.5	32.64		343870	2551	41.39	

4s - 4p  $\rightarrow$  F. Bredice, M. Gallardo, and J. G. Reyna Almandos, "Revised Analysis of Triply Ionized Argon (Ar IV)", *Phys. Scr.* 51, 446 (1995).